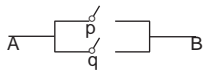


# STATEMENTS AND SETS

- The terms which connect two statements are called \_\_\_\_\_
- If the switch 'P' is 'OFF' we represent it by \_\_\_\_\_
- The complement law using ' $\wedge$ ' is \_\_\_\_\_
- The truth value of  $(3 \neq 2) \vee (2 = 3)$  is \_\_\_\_\_
- The statement of the form "If..... then....." is called an \_\_\_\_\_
- A combination of one or more simple statements with a connective is called a \_\_\_\_\_
- The symbol for existential quantifier \_\_\_\_\_ (June 2009), (June 2008)
- $\sim(p \Leftrightarrow q) =$  \_\_\_\_\_
- The contrapositive of "If a polygon is a square then it is a rectangle" is \_\_\_\_\_
- p, q, r are three statements then  $p \wedge (q \vee r) = (p \wedge q) \vee (p \wedge r)$  is \_\_\_\_\_ law
- "For all" or "For every" is called \_\_\_\_\_ quantifier.
- If p and q are switches. The combination of  $p \vee q$  is called \_\_\_\_\_



- p and q are two statements. The symbolic form of "Converse of a conditional is equivalent to its inverse" is \_\_\_\_\_
- The statement which uses the connective "OR" is called a \_\_\_\_\_
- The truth value of  $(4 \times 7 = 20) \Leftrightarrow (4 \div 7 = 1)$  is \_\_\_\_\_
- P is the statement then  $\sim(\sim(p))$  is \_\_\_\_\_
- The symbolic form of "If x is not odd then  $x^2$  is odd" \_\_\_\_\_
- p: It is raining, q: The sun is shining . Connect p,q using conjunction is \_\_\_\_\_
- Denial of a statement is called its \_\_\_\_\_
- p and q are two statements then example for tautology is \_\_\_\_\_
- $p \wedge (\sim p)$  is very simple example of a \_\_\_\_\_ (June 2009)
- $\sim(p \vee q) \equiv$  \_\_\_\_\_ (June 2009)
- $P \vee p = p$ . This is \_\_\_\_\_ law. (June 2010)
- The symbol of Universal Quantifier is \_\_\_\_\_ (March 2009)
- $\sim(p \vee q) \equiv (\sim p) \wedge (\sim q)$  is \_\_\_\_\_ law. (June 2008)
- $p \vee (q \wedge r) \equiv (p \vee r) \wedge (p \vee q)$  is \_\_\_\_\_ law. (March 2008)
- The truth value of implication statement :  
If  $3 \div 2 = 5$  then  $1 \times 0 = 0$  is \_\_\_\_\_ (March 2008)
- The last column of truth table contains only F it is called \_\_\_\_\_
- p or not p is example for \_\_\_\_\_
- The inverse of " $\sim p \Rightarrow \sim q$ " is \_\_\_\_\_

## KEY

- |                            |                    |   |   |                                 |
|----------------------------|--------------------|---|---|---------------------------------|
| 1. Connectivities          | 2. $P^1$           | 3. $(p \wedge (\sim p)) \equiv f$                             | 4. True   | 5. conditional (or) implication |
| 6. Compound statement      | 7. $\exists$ ;     | 8. $\sim p \Leftrightarrow q$ (or) $p \Leftrightarrow \sim q$ | 9. If a polygon is not a rectangle then it is not a square. |                                 |
| 10. Distributive law.      | 11. Universal      | 12. Parallel combination                                      | 13. $(q \Rightarrow p) \equiv \sim(p \Rightarrow q)$        |                                 |
| 14. Disjunction            | 15. True           | 16. $\sim p$  | 17. "x is not odd $\Rightarrow x^2$ is odd"                 |                                 |
| 18. $p \wedge q$           | 19. Negation       | 20. $p \vee (\sim q)$   | 21. contradiction   |                                 |
| 22. $\sim p \wedge \sim q$ | 23. idempotent law | 24. $\forall$   | 25. De morgan's law   |                                 |
| 26. distributive law       | 27. True           | 28. contradiction   | 29. Tautology   | 30. $p \Rightarrow q$           |

## SETS

- If A and B are disjoint sets, then  $n(A \cup B) =$  \_\_\_\_\_ (June 2009)
- If  $A \subset B$  then  $A \cap B =$  \_\_\_\_\_ (June 2009)
- The complement of  $\mu$  is \_\_\_\_\_ (March 2009)
- $n(\phi) =$  \_\_\_\_\_ (March 2009)
- If  $A \subset B$  then  $A \cup B =$  \_\_\_\_\_ (June 2008)
- If  $A \subseteq B$  and  $B \subseteq A$  then \_\_\_\_\_ (June 2008)
- $A \cup A' =$  \_\_\_\_\_ (June 2008)
- If  $A \subset B$  and  $n(A) = 5$ ,  $n(B) = 6$  then  $n(A \cup B) =$  \_\_\_\_\_ (March 2008)
- The set builder form of  $B = \{1, 8, 27, 64, 125\}$  is \_\_\_\_\_ (March 2008)
- $(A \cup B)' =$  \_\_\_\_\_ (March 2010)
- If  $A = \{3, 4\}$ ,  $B = \{4, 5\}$  then  $n(A \times B) =$  \_\_\_\_\_
- $(A \cap B) \cup (A \cap C) =$  \_\_\_\_\_
- If A and B are two sets then  $A \Delta B =$  \_\_\_\_\_
- If  $A \subset B$ ,  $n(A) = 10$  and  $n(B) = 15$  then  $n(A - B) =$  \_\_\_\_\_
- If  $A \cap B = \phi$ ,  $n(A \cup B) = 12$  then  $n(A \Delta B) =$  \_\_\_\_\_

16. If A, B, C are three sets  $A - (B \cup C) =$  \_\_\_\_\_
17.  $n(A \cup B) = 8$ ,  $n(A \cap B) = 2$ ,  $n(B) = 3$  then  $n(A) =$  \_\_\_\_\_
18. If  $A = \{x; x \leq 5, x \in \mathbb{N}\}$ ,  $B = \{2, 3, 6, 8\}$  then  $A \cap B =$  \_\_\_\_\_
19. If A, B are disjoint sets  $n(A) = 4$ ,  $n(A \cup B) = 12$  then  $n(B) =$  \_\_\_\_\_
20.  $(A \cup B)' = A' \cap B'$  is \_\_\_\_\_ law.
21. A, B are two sets then  $x \notin (A - B) =$  \_\_\_\_\_
22.  $A \subset B$  and  $n(A) = 5$ ,  $n(B) = 6$  then  $n(A \cup B) =$  \_\_\_\_\_
23. The sets which are having same cardinal numbers are called \_\_\_\_\_
24. If A has 'n' elements then the number of elements in proper sub set is \_\_\_\_\_
25. If A and B are disjoint sets then  $n(A \cap B) =$  \_\_\_\_\_
26. If  $n(A) = 7$ ,  $n(B) = 5$  then the maximum number of elements in  $A \cap B$  is \_\_\_\_\_
27. If  $A \cap B = \phi$  then  $B \cap A =$  \_\_\_\_\_
28. If any law of quality of sets, if we interchange  $\cap$  and  $\cup$  and  $\mu$  and  $\phi$  the resulting law also true, this is known as \_\_\_\_\_
29.  $A - B' =$  \_\_\_\_\_
30. A, B are subsets of  $\mu$  then  $A \cap B' =$  \_\_\_\_\_

## KEY

- |  |                     |                            |                         |   |                     |                                |                          |
|--|---------------------|----------------------------|-------------------------|---|---------------------|--------------------------------|--------------------------|
| 1. $n(A) + n(B)$                               | 2. A                | 3. $\phi$                  | 4. 0                    | 5. B  | 6. $A = B$          | 7. $\mu$                       | 8. 6                     |
| 9. $\{x/x = n^3, n \in \mathbb{N}, n \leq 5\}$ | 10. $A' \cap B'$    | 11. 4                      | 12. $A \cap (B \cup C)$ | 13. $(A \cup B) - (A \cap B)$ (or) $(A - B) \cup (B - A)$ | 20. De Morgan's law | 21. $x \notin A$ and $x \in B$ | 28. Principle of duality |
| 14. 0  | 15. 12              | 16. $(A - B) \cap (A - C)$ | 17. 7                   | 18. $\{2, 3\}$  | 19. 8               | 26. 5                          | 27. B                    |
| 22. 6  | 23. equivalent sets | 24. $2^n - 2$              | 25. 0                   |   |                     |                                |                          |
| 29. $A \cap B$                                 | 30. A - B           |                            |                         |   |                     |                                |                          |

### STATEMENTS AND SETS: Important Questions

#### 4 Marks

1. Using element wise prove that  $A - (B \cap C) = (A - B) \cup (A - C)$
2. Prove that  $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
3. Let A, B are two subsets of a Universal set  $\mu$  show that  $A \cap B = A - B^1 = B - A^1$
4. Prove that  $(A \wedge B)^1 = A^1 \cup B^1$

#### 2 Marks

1. Define implication and write truth table?
2. Write the truth table  $(\sim P) \vee (P \wedge q)$ .
3. Write the converse, inverse and contrapositive of the conditional "If in a triangle ABC,  $AB > AC$  then  $\angle C > \angle B$ ."
4. If  $A \cap B = \phi$  then show that  $B \cap A^1 = B$
5. Using element wise proof show that  $A - B = A \cap B^1$
6. If A, B are any two sets, prove that  $A^1 - B^1 = B - A$
7. Show that  $A \cup B = \phi$ , implies  $A = \phi$  and  $B = \phi$ .

#### 1 Mark

1. Define Tautology and contradiction?
2. Write Truth table for conjunction?
3. Prove that  $(A^1)^1 = A$
4. Write contrapositive of a conditional 'If two triangles are congruent then they are similar'.
5. Show that  $P \wedge (\sim P)$  is contradiction.
6. If  $A = \{1, 2, 3\}$ ,  $B = \{2, 3, 4\}$  then find  $A \Delta B$ .
7. Write set-builder form of  $A = \left\{1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \frac{1}{5}, \frac{1}{6}\right\}$
8. Prove that  $A \wedge B \subset A$  for any two sets A, B.
9. Prove that  $\sim(\sim P) = P$