

MODEL QUESTION PAPER
MATHEMATICS – Paper II B
(Coordinate Geometry and Calculus)

Time : 3 Hours

Max Marks : 75

Section – A

- I. Very Short Answer Questions 10x2=20 Marks
Attempt all Questions. Each Question carries 2 marks.
1. If $x^2 + y^2 - 4x + 6y + c = 0$ represents a circle with radius '6', find the value of 'c'.
 2. Find the equation of the directrix of the parabola $2x^2 + 7y = 0$.
 3. Find the length of the latus rectum of the ellipse $\frac{x^2}{16} + \frac{y^2}{8} = 1$
 4. Find the eccentricity of the hyperbola $x^2 - 4y^2 = 4$
 5. Find the distance between the two points in a plane whose polar coordinates are $(2, \pi/6)$ $(3, \pi/4)$
 6. If $y = \frac{1}{2x+5}$, then find y_n .
 7. Find $\int \sqrt{1 + \sin 2x} \, dx$
 8. Find $\int \frac{e^{\sin^{-1} x}}{\sqrt{1-x^2}} \, dx$

9. Obtain $\int_1^4 x \sqrt{x^2 - 1} \, dx$

10. State the Simpson's rule for Numerical Integration of a function $f(x)$ over the interval $[a, b]$ by dividing $[a, b]$ into n sub-intervals.

Section – B

- II. Short Answer Questions 5 x 4 = 20 Marks

Attempt any five questions. Each question carries 4 marks

11. If the line $y = mx + c$ touches the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$

$c^2 = a^2 m^2 + b^2 ; (a > b)$

12. Find the equations of the tangents shown drawn from $(-2, 1)$ to the hyperbola $2x^2 - 3y^2 = 6$.

13. Transform the polar equation $r \cos^2 \theta = a$ ($a > 0$), origin as pole and the

2

+ve axis as initial line, into Cartesian form.

14. If $y = \frac{\log x}{x}$ then show that

$$y_n = \frac{(-1)^n \cdot n!}{x^{n+1}} \left(\log x - 1 - \frac{1}{2} - \frac{1}{3} - \dots - \frac{1}{n} \right)$$

15. Evaluate $\int \frac{x^6 - 1}{1 + x^2} dx$
16. Solve $(x^2 + y^2) dx = 2xy dy$
17. Solve $\frac{dy}{dx} = \frac{2x + y + 3}{2y + x + 1}$

Section – C

- II. Long Answer Questions 5 x 7 = 35 Marks

Attempt any five questions. Each question carries 7 marks

18. Find the equation of the pair of tangents drawn from (3,2) to the circle $x^2 + y^2 - 6x + 4y - 2 = 0$
19. Find the equation of the circle passing through the points of intersection of the circles $x^2 + y^2 - 8x - 6y + 21 = 0$, $x^2 + y^2 - 2x - 15 = 0$ and the point (1,2).
20. Find the equation of the circle passing through the origin and coaxial with the circles $x^2 + y^2 - 6x + 4y - 8 = 0$ and $x^2 + y^2 - 2x + y + 4 = 0$.
21. Find the pole of the line $x + y + 2 = 0$ with respect to the parabola $y^2 + 4x - 2y - 3 = 0$.

22. Evaluate $\int \frac{3 \sin x + \cos x + 7}{\sin x + \cos x + 1} dx$

23. Evaluate $\int \frac{x^{1/4}}{x^{1/2} + 1} dx$

24. Find the area enclosed by the curves $y = 3x$ and $y = 6x - x^2$.

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QUESTION PAPER PATTERN

Subject : **Mathematics**
 Paper : Paper –II B
 Class : II Year Intermediate
 (Coordinate Geometry, Calculus)
 Time : 3 Hours
 Max. Marks : 75

1. Weightage of Objectives :

| Objectives | Knowledge | Understanding | Application | Total |
|--------------|-----------|---------------|-------------|-------|
| Actual Marks | 41 | 28 | 28 | 97 |

2. Weightage to form of Questions :

| Form of questions | VSA Sec A | SA Sec B | LA Sec C | Total |
|-------------------|---|---------------------------------------|---------------------------------------|----------|
| No. of questions | 10 of 10 | 5 of 7 | 5 of 7 | 20 of 24 |
| Marks allotted | $\frac{10 \times 2=20}{10 \times 2=20}$ | $\frac{5 \times 4=20}{7 \times 4=28}$ | $\frac{5 \times 7=35}{7 \times 7=49}$ | 75 / 97 |

3. Weightage to content units / sub-units :

Coordinate Geometry

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|----------------------|----|
| 1. Circles | 16 |
| 2. System of Circles | 07 |
| 3. Parabola | 09 |
| 4. Ellipse | 06 |
| 5. Hyperbola | 06 |
| 6. Polar Coordinates | 06 |

Calculus

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|-------------------------------|----|
| 7. Successive differentiation | 06 |
| 8. Integration | 15 |
| 9. Definite Integration | 09 |
| 10. Numerical Integration | 09 |
| 11. Differential equations | 08 |

Total 97

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