

1. A function f from the set of natural numbers to integers defined by

$$f(n) = \begin{cases} \frac{n-1}{2}, & \text{when } n \text{ is odd} \\ -\frac{n}{2}, & \text{when } n \text{ is even} \end{cases}$$

is :

- (a) one-one but not onto
- (b) onto but not one-one
- (c) one-one and onto both
- (d) neither one-one nor onto

2. Let z_1 and z_2 be two roots of the equation $z^2 + az + b = 0$, z being complex. Further, assume that the origin, z_1 and z_2 form an equilateral triangle. Then :

- (a) $a^2 = b$
- (b) $a^2 = 2b$
- (c) $a^2 = 3b$
- (d) $a^2 = 4b$

3. If z and ω are two non-zero complex numbers such that $|z\omega| = 1$, and

$\arg(z) - \arg(\omega) = \frac{\pi}{2}$, then $\bar{z}\omega$ is equal to :

- (a) 1
- (b) -1
- (c) i
- (d) $-i$

4. If $\left(\frac{1+i}{1-i}\right)^x = 1$, then :

- (a) $x = 4n$, where n is any positive integer
- (b) $x = 2n$, where n is any positive integer
- (c) $x = 4n + 1$, where n is any positive integer
- (d) $x = 2n + 1$, where n is any positive integer

5. If $\begin{vmatrix} a & a^2 & 1+a^3 \\ b & b^2 & 1+b^3 \\ c & c^2 & 1+c^3 \end{vmatrix} = 0$

and vectors $(1, a, a^2)$, $(1, b, b^2)$ and $(1, c, c^2)$ are non-coplanar, then the product abc equals :

- (a) 2
- (b) -1
- (c) 1
- (d) 0

6. If the system of linear equations

$$\begin{aligned} x + 2ay + az &= 0 \\ x + 3by + bz &= 0 \\ x + 4cy + cz &= 0 \end{aligned}$$

has a non-zero solution, then a, b, c :

- (a) are in AP
- (b) are in GP
- (c) are in HP
- (d) satisfy $a + 2b + 3c = 0$

7. If the sum of the roots of the quadratic equation $ax^2 + bx + c = 0$ is equal to the sum of the squares of their reciprocals, then $\frac{a}{c}, \frac{b}{a}$ and $\frac{c}{b}$ are in :

- (a) arithmetic progression
- (b) geometric progression
- (c) harmonic progression
- (d) arithmetico-geometric progression

8. The number of the real solutions of the equation $x^2 - 3|x| + 2 = 0$ is :

- (a) 2
- (b) 4
- (c) 1
- (d) 3

9. The value of ' a ' for which one root of the quadratic equation

$$(a^2 - 5a + 3)x^2 + (3a - 1)x + 2 = 0$$

is twice as large as the other, is :

- (a) $2/3$
- (b) $-2/3$
- (c) $1/3$
- (d) $-1/3$

10. If $A = \begin{bmatrix} a & b \\ b & a \end{bmatrix}$ and $A^2 = \begin{bmatrix} \alpha & \beta \\ \beta & \alpha \end{bmatrix}$, then :

- (a) $\alpha = a^2 + b^2$, $\beta = ab$
- (b) $\alpha = a^2 + b^2$, $\beta = 2ab$
- (c) $\alpha = a^2 + b^2$, $\beta = a^2 - b^2$
- (d) $\alpha = 2ab$, $\beta = a^2 + b^2$

11. A student is to answer 10 out of 13 questions in an examination such that he must choose at least 4 from the first five questions. The number of choices available to him is :

- (a) 140
- (b) 196
- (c) 280
- (d) 346

12. The number of ways in which 6 men and 5 women can dine at a round table, if no two women are to sit together, is given by :

- (a) $6! \times 5!$
- (b) 30
- (c) $5! \times 4!$
- (d) $7! \times 5!$

13. If $1, \omega, \omega^2$ are the cube roots of unity, then :

$$\Delta = \begin{vmatrix} 1 & \omega^n & \omega^{2n} \\ \omega^n & \omega^{2n} & 1 \\ \omega^{2n} & 1 & \omega^n \end{vmatrix}$$

is equal to :

- (a) 0
- (b) 1
- (c) ω
- (d) ω^2

14. If ${}^n C_r$ denotes the number of combinations of n things taken r at a time, then the expression ${}^n C_{r+1} + {}^n C_{r-1} + 2 \times {}^n C_r$ equals :
- (a) ${}^{n+2} C_r$ (b) ${}^{n+2} C_{r+1}$
 (c) ${}^{n+1} C_r$ (d) ${}^{n+1} C_{r+1}$
15. The number of integral terms in the expansion of $(\sqrt{3} + \sqrt[8]{5})^{256}$ is :
- (a) 32 (b) 33
 (c) 34 (d) 35
16. If x is positive, the first negative term in the expansion of $(1+x)^{27/5}$ is :
- (a) 7th term (b) 5th term
 (c) 8th term (d) 6th term
17. The sum of the series $\frac{1}{1 \cdot 2} - \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} - \dots$ upto ∞ is equal to :
- (a) $2 \log_e 2$ (b) $\log_e 2 - 1$
 (c) $\log_e 2$ (d) $\log_e \left(\frac{4}{e}\right)$
18. Let $f(x)$ be a polynomial function of second degree. If $f(1) = f(-1)$ and a, b, c are in AP, then $f'(a), f'(b)$ and $f'(c)$ are in :
- (a) AP (b) GP
 (c) HP (d) arithmetico-geometric progression
19. If x_1, x_2, x_3 and y_1, y_2, y_3 are both in GP with the same common ratio, then the points (x_1, y_1) , (x_2, y_2) and (x_3, y_3) :
- (a) lie on a straight line (b) lie on an ellipse
 (c) lie on a circle (d) are vertices of a triangle
20. The sum of the radii of inscribed and circumscribed circles for an n sided regular polygon of side a , is :
- (a) $a \cot\left(\frac{\pi}{n}\right)$ (b) $\frac{a}{2} \cot\left(\frac{\pi}{2n}\right)$
 (c) $a \cot\left(\frac{\pi}{2n}\right)$ (d) $\frac{a}{4} \cot\left(\frac{\pi}{2n}\right)$
21. If in a triangle ABC
- $$a \cos^2\left(\frac{C}{2}\right) + c \cos^2\left(\frac{A}{2}\right) = \frac{3b}{2},$$
- then the sides a, b and c :
- (a) are in AP (b) are in GP
 (c) are in HP (d) satisfy $a + b = c$
22. In a triangle ABC , medians AD and BE are drawn. If $AD = 4$, $\angle DAB = \frac{\pi}{6}$ and $\angle ABE = \frac{\pi}{3}$, then the area of the $\triangle ABC$ is :
- (a) $8/3$ (b) $16/3$
 (c) $32/3$ (d) $64/3$
23. The trigonometric equation $\sin^{-1} x = 2 \sin^{-1} a$, has a solution for :
- (a) $\frac{1}{2} < |a| < \frac{1}{\sqrt{2}}$ (b) all real values of a
 (c) $|a| < \frac{1}{2}$ (d) $|a| \geq \frac{1}{\sqrt{2}}$
24. The upper $3/4$ th portion of a vertical pole subtends an angle $\tan^{-1} 3/5$ at a point in the horizontal plane through its foot and at a distance 40 m from the foot. A possible height of the vertical pole is :
- (a) 20 m (b) 40 m
 (c) 60 m (d) 80 m
25. The real number x when added to its inverse gives the minimum value of the sum at x equals to :
- (a) 2 (b) 1
 (c) -1 (d) -2
26. If $f : R \rightarrow R$ satisfies $f(x+y) = f(x) + f(y)$, for all $x, y \in R$ and $f(1) = 7$, then $\sum_{r=1}^n f(r)$ is :
- (a) $\frac{7n}{2}$ (b) $\frac{7(n+1)}{2}$
 (c) $7n(n+1)$ (d) $\frac{7n(n+1)}{2}$
27. If $f(x) = x^n$, then the value of
- $$f(1) - \frac{f'(1)}{1!} + \frac{f''(1)}{2!} - \frac{f'''(1)}{3!} + \dots + \frac{(-1)^n f^{(n)}(1)}{n!}$$
- is :
- (a) 2^n (b) 2^{n-1}
 (c) 0 (d) 1
28. Domain of definition of the function
- $$f(x) = \frac{3}{4-x^2} + \log_{10}(x^3 - x)$$
- is :
- (a) $(1, 2)$ (b) $(-1, 0) \cup (1, 2)$
 (c) $(1, 2) \cup (2, \infty)$ (d) $(-1, 0) \cup (1, 2) \cup (2, \infty)$
29. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\left[1 - \tan\left(\frac{x}{2}\right)\right][1 - \sin x]}{\left[1 + \tan\left(\frac{x}{2}\right)\right][\pi - 2x]^3}$ is :
- (a) $\frac{1}{8}$ (b) 0
 (c) $\frac{1}{32}$ (d) ∞
30. If $\lim_{x \rightarrow 0} \frac{\log(3+x) - \log(3-x)}{x} = k$, the value of k is :
- (a) 0 (b) $-1/3$
 (c) $2/3$ (d) $-2/3$

One observation that was 20, was found to be wrong and was replaced by the correct value 30. Then the corrected variance is :

67. Five horses are in a race. Mr. A selects two of the horses at random and bets on them. The probability that Mr. A selected the winning horse, is :

- (a) $\frac{4}{5}$ (b) $\frac{3}{5}$
 (c) $\frac{1}{5}$ (d) $\frac{2}{5}$

- 68.** Events A, B, C are mutually exclusive events such that $P(A) = \frac{3x+1}{3}$, $P(B) = \frac{1-x}{4}$ and $P(C) = \frac{1-2x}{2}$. The set of possible values of x are in the interval :

- (a) $\left[\frac{1}{3}, \frac{1}{2} \right]$ (b) $\left[\frac{1}{3}, \frac{2}{3} \right]$
 (c) $\left[\frac{1}{3}, \frac{13}{3} \right]$ (d) $[0, 1]$

69. The mean and variance of a random variable X having a binomial distribution are 4 and 2 respectively, then $P(X = 1)$ is :

- (a) $\frac{1}{32}$ (b) $\frac{1}{16}$
 (c) $\frac{1}{8}$ (d) $\frac{1}{4}$

70. The resultant of forces \vec{P} and \vec{Q} is \vec{R} . If \vec{Q} is doubled, then \vec{R} is doubled. If the direction of \vec{Q} is reversed, then \vec{R} is again doubled, then $P^2 : Q^2 : R^2$ is :

- (a) 3 : 1 : 1 (b) 2 : 3 : 2
 (c) 1 : 2 : 3 (d) 2 : 3 : 1

71. Let R_1 and R_2 respectively be the maximum ranges up and down an inclined plane and R be the maximum range on the horizontal plane. Then R_1, R, R_2 are in :

- (a) arithmetico-geometric progression (AGP)
 - (b) AP
 - (c) GP
 - (d) HP

72. A couple is of moment \vec{G} and the force forming the couple is \vec{P} . If \vec{P} is turned through a right angle, the moment of the couple thus formed is \vec{H} . If instead, the forces \vec{P} is turned through an angle α , then the moment of couple becomes :

- (a) $\vec{G} \sin \alpha - \vec{H} \cos \alpha$
 (b) $\vec{H} \cos \alpha + \vec{G} \sin \alpha$
 (c) $\vec{G} \cos \alpha + \vec{H} \sin \alpha$
 (d) $\vec{H} \sin \alpha - \vec{G} \cos \alpha$

73. Two particles start simultaneously from the same point and move along two straight lines, one with uniform velocity \vec{u} and the other from rest with uniform acceleration \vec{f} . Let α be the angle between their directions of motion. The relative velocity of the second particle w.r.t. the first is least after a time :

- (a) $\frac{u \sin \alpha}{f}$ (b) $\frac{f \cos \alpha}{u}$
 (c) $u \sin \alpha$ (d) $\frac{u \cos \alpha}{f}$

74. Two stones are projected from the top of a cliff h metres high, with the same speed u so as to hit the ground at the same spot. If one of the stones is projected horizontally and the other is projected at an angle θ to the horizontal, then tan θ equals :

- (a) $\sqrt{\frac{2u}{gh}}$ (b) $2g \sqrt{\frac{u}{h}}$
 (c) $2h \sqrt{\frac{u}{g}}$ (d) $u \sqrt{\frac{2}{gh}}$

75. A body travels a distance s in t seconds. It starts from rest and ends at rest. In the first part of the journey, it moves with constant acceleration f and in the second part with constant retardation r . The value of t is given by :

- (a) $2s \left(\frac{1}{f} + \frac{1}{r} \right)$ (b) $\frac{2s}{\frac{1}{f} + \frac{1}{r}}$
 (c) $\sqrt{2s(f+r)}$ (d) $\sqrt{2s \left(\frac{1}{f} + \frac{1}{r} \right)}$

ANSWERS

PHYSICS AND CHEMISTRY

1. (b)	2. (a)	3. (b)	4. (a)	5. (d)	6. (a)	7. (a)	8. (d)
9. (c)	10. (b)	11. (a)	12. (c)	13. (c)	14. (d)	15. (c)	16. (a)
17. (a)	18. (c)	19. (c)	20. (b)	21. (c)	22. (d)	23. (d)	24. (b)
25. (d)	26. (a)	27. (d)	28. (c)	29. (c)	30. (b)	31. (d)	32. (a)
33. (d)	34. (c)	35. (c)	36. (a)	37. (c)	38. (d)	39. (a)	40. (d)
41. (c)	42. (a)	43. (d)	44. (a)	45. (b)	46. (a)	47. (a)	48. (b)
49. (b)	50. (c)	51. (c)	52. (d)	53. (b)	54. (d)	55. (c)	56. (b)
57. (b)	58. (a)	59. (c)	60. (a)	61. (d)	62. (b)	63. (c)	64. (a)
65. (a)	66. (b)	67. (a)	68. (d)	69. (b)	70. (c)	71. (c)	72. (a)
73. (b)	74. (d)	75. (d)	76. (b)	77. (a)	78. (b)	79. (a)	80. (b)
81. (b)	82. (c)	83. (d)	84. (d)	85. (b)	86. (c)	87. (a)	88. (b)
89. (d)	90. (b)	91. (c)	92. (c)	93. (c)	94. (b)	95. (c)	96. (b)
97. (b)	98. (c)	99. (b)	100. (c)	101. (a)	102. (b)	103. (c)	104. (a)
105. (d)	106. (a)	107. (d)	108. (d)	109. (c)	110. (b)	111. (a)	112. (c)
113. (d)	114. (b)	115. (b)	116. (c)	117. (a)	118. (c)	119. (a)	120. (b)
121. (b)	122. (a)	123. (d)	124. (b)	125. (b)	126. (b)	127. (a)	128. (d)
129. (c)	130. (a)	131. (b)	132. (b)	133. (c)	134. (c)	135. (d)	136. (b)
137. (a)	138. (d)	139. (a)	140. (c)	141. (a)	142. (b)	143. (c)	144. (a)
145. (a)	146. (d)	147. (d)	148. (c)	149. (d)	150. (c)		

MATHEMATICS

1. (c)	2. (c)	3. (d)	4. (a)	5. (b)	6. (c)	7. (c)	8. (b)
9. (a)	10. (b)	11. (b)	12. (a)	13. (a)	14. (b)	15. (b)	16. (c)
17. (d)	18. (a)	19. (a)	20. (b)	21. (a)	22. (*)	23. (a)	24. (b)
25. (c)	26. (d)	27. (c)	28. (d)	29. (c)	30. (c)	31. (a)	32. (b)
33. (b)	34. (c)	35. (b)	36. (b)	37. (c)	38. (c)	39. (d)	40. (d)
41. (c)	42. (c)	43. (b)	44. (b)	45. (a)	46. (b)	47. (d)	48. (d)
49. (a)	50. (c)	51. (a)	52. (c)	53. (a)	54. (c)	55. (c)	56. (d)
57. (c)	58. (d)	59. (b)	60. (b)	61. (*)	62. (c)	63. (c)	64. (d)
65. (d)	66. (a)	67. (d)	68. (a)	69. (a)	70. (b)	71. (d)	72. (c)
73. (d)	74. (d)	75. (d)					

(*) No option is correct in question paper.