

II B.Tech II Semester Examinations, APRIL 2011
FORMAL LANGUAGES AND AUTOMATA THEORY
Computer Science And Engineering

Time: 3 hours

Max Marks: 75

Answer any FIVE Questions
All Questions carry equal marks

1. (a) Construct DFA and NFA accepting the set of all strings not containing 101 as a substring.
 (b) Draw the transition diagram of a FA which accepts all strings of 1's and 0's in which both the number of 0's and 1's are even.
 (c) Define NFA with an example. [6+5+4]

2. Discuss about
 - (a) Context Free Grammar
 - (b) Left most derivation
 - (c) Right most derivation
 - (d) Derivation tree. [15]

3. (a) If $G = (\{S\}, \{0, 1\}, \{S \rightarrow 0S1, S \rightarrow \varepsilon\}, S)$, find $L(G)$.
 (b) If $G = (\{S\}, \{a\}, \{S \rightarrow SS\}, S)$ find the language generated by G . [7+8]

4. (a) What is unrestricted grammar? Give an Example.
 (b) Explain the language generated by unrestricted grammar.
 (c) Write about the machine corresponding to unrestricted grammar. [5+5+5]

5. (a) Construct a DFA with reduced states equivalent to the regular expression $10 + (0 + 11)0^* 1$.
 (b) Prove $(a + b)^* = a^*(ba^*)^*$ [7+8]

6. (a) Construct a Mealy machine which can output EVEN, ODD according as the total number of 1's encountered is even or odd. The input symbols are 0 and 1.
 (b) Construct Moore machine equivalent to Mealy machine described in (a). [8+7]

7. (a) Convert the following Push Down Automata to Context Free Grammar
 $M = (\{q_0, q_1\}, \{a, b\}, \{z_0, z_a\}, \delta, q_0, z_0, \varphi)$
 δ is given by
 $\delta(q_0, a, z_0) = (q_0, z_a z_0)$
 $\delta(q_0, a, z_a) = (q_0, z_a z_a)$
 $\delta(q_0, b, z_a) = (q_1, \varepsilon)$
 $\delta(q_1, b, z_a) = (q_1, \varepsilon)$
 $\delta(q_1, \varepsilon, z_0) = (q_1, \varepsilon)$

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- (b) Write the corresponding language for above Push Down Automata. [13+2]
8. Design Turing Machine to increment the value of any binary number by one. The out put should also be a binary number with value one more the number given. [15]

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1. (a) Define NFA with ϵ moves.
 (b) differentiate Moore and Mealy machines.
 (c) Write the steps in minimization of FA. [4+5+6]
2. (a) Write and explain the properties of transition function.
 (b) Prove that for any transition function δ and for any two input strings x and y , $\delta(q, xy) = \delta(\delta(q, x), y)$.
 (c) Define Finite Automata and Transition diagram. [6+5+4]
3. Describe, in the English language, the sets represented by the following regular expressions:
 (a) $a(a+b)^*ab$
 (b) $a^*b + b^*a$ [15]
4. (a) What is type1 grammar? Give an Example.
 (b) Explain the language generated by type1 grammar.
 (c) Write about the machine corresponding to type1 grammar. [5+5+5]
5. Design Turing Machine for $L = \{ a^n b^n c^n \mid n \geq 1 \}$. [15]
6. (a) Let G be the grammar. $S \rightarrow aS \mid aSbS \mid \epsilon$. Prove that $L(G) = \{x \mid \text{such that each prefix of } x \text{ has atleast as many } a\text{'s as } b\text{'s}\}$
 (b) Show that $\{abc, bca, cab\}$ can be generated by a regular grammar whose terminal set is $\{a, b, c\}$ [8+7]
7. (a) Show that the grammar is ambiguous
 $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$.
 (b) Find Context Free Grammar for $L = \{a^i b^j c^k \mid j=i \text{ or } j=k\}$. [7+8]
8. Which of the following are CFL's? explain
 (a) $\{a^i b^j \mid i \neq j \text{ and } i \neq 2j\}$
 (b) $\{a^i b^j \mid i \geq 1 \text{ and } j \geq 1\}$
 (c) $\{(a+b)^* - \{a^n b^n \mid n \geq 1\}\}$
 (d) $\{a^n b^n c^m \mid n \leq m \leq 2n\}$. [15]

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1. Describe the following sets by regular expressions
 - (a) $\{101\}$
 - (b) $\{abba\}$
 - (c) $\{01,10\}$
 - (d) $\{a, ab\}$ [15]

2. (a) Draw the transition diagram for a NFA which accepts all strings with either two consecutive 0's or two consecutive 1's.
- (b) differentiate NFA and DFA.
- (c) Construct DFA accepting the set of all strings with atmost one pair of consecutive 0's and atmost one pair of consecutive 1's. [6+4+5]

3. State and explain about closure properties of Context Free Languages. [15]

4. Obtain Chomsky Normal form for following Context Free Grammar
 $S \rightarrow \sim S \mid [S > S] \mid p \mid q.$ [15]

5. (a) Construct a NFA accepting $\{ab, ba\}$ and use it to find a deterministic automaton accepting the same set.
- (b) $M = (\{q_1, q_2, q_3\}, \{0, 1\}, \delta, q_1, \{q_3\})$ is a NFA where δ is given by

$$\begin{aligned} \delta(q_1, 0) &= \{q_2, q_3\}, & \delta(q_1, 1) &= \{q_1\} \\ \delta(q_2, 0) &= \{q_1, q_2\}, & \delta(q_2, 1) &= \emptyset \\ \delta(q_3, 0) &= \{q_2\}, & \delta(q_3, 1) &= \{q_1, q_2\} \end{aligned}$$
 construct an equivalent DFA. [7+8]

6. (a) Design Turing Machine over $\{0,1\}$, $L = \{w \mid |w| \text{ is a multiple of } 3\}$.
- (b) Draw the transition diagram for above language. [11+4]

7. (a) Find the language generated by the grammar. $S \rightarrow 0A \mid 1S \mid 0 \mid 1$, $A \rightarrow 1A \mid 1S \mid 1$
- (b) Construct context-free grammars to generate the set $\{a^l b^m c^n \mid \text{one of } l, m, n \text{ equals } 1 \text{ and the remaining two are equal}\}$. [7+8]

8. Construct LR(0) items for the grammar given find it's equivalent DFA.
 $S' \rightarrow S$
 $S \rightarrow AS \mid a$
 $A \rightarrow aA \mid b$ [15]

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1. Find regular expressions representing the following sets
 - (a) the set of all strings over $\{0, 1\}$ having at most one pair of 0's or at most of one pair of 1's
 - (b) the set of all strings over $\{a, b\}$ in which the number of occurrences of a is divisible by 3
 - (c) the set of all strings over $\{a, b\}$ in which there are at least two occurrences of b between any two occurrences of a.
 - (d) the set of all strings over $\{a, b\}$ with three consecutive b's.

[15]

2. (a) What is generating variable? Give example.
 (b) Reduce the following Context Free Grammar

$$S \rightarrow aAa$$

$$A \rightarrow sb / bCC / DaA$$

$$C \rightarrow abb / DD$$

$$E \rightarrow aC$$

$$D \rightarrow aDA$$

[4+11]

3. Construct
 - (a) A context-free but not regular grammar.
 - (b) A regular grammar to generate $\{a^n \mid n \geq 1\}$.

[15]

4. (a) Construct a transition system which can accept strings over the alphabet a, b, containing either cat or rat.
 (b) Show that there exist no finite automaton accepting all palindromes over $\{a, b\}$.

[7+8]

5. Design Push Down Automata for the language $L = \{wcw^R \mid w \in (0+1)^*\}$.

[15]

6. Consider the grammar given below

$$S \rightarrow Aa$$

$$A \rightarrow AB \mid \varepsilon$$

$$B \rightarrow aB \mid b$$
 - (a) Find the CLOSURE ($S' \rightarrow .S$)
 - (b) GOTO($\{A \rightarrow .AB\}, [B \rightarrow .aB], A$)

[7+8]

7. (a) Draw the transition diagram and transition table of FA which accept the set of all strings over the alphabet $\{0, 1\}$ with equal number of 0's and 1's such that each prefix has atmost one more 0 than 1's and atmost one more 1 than 0's.
- (b) Draw transition diagram and transition table of NFA which accepts the set of all strings over an alphabet $\{0, 1\}$, beginning with a '1' which, interpreted as the binary representation of an integer is congruent to 0 modulo 5. And construct an equivalent DFA. [6+9]
8. Design Turing Machine to find 2's complement of a given binary number. [15]
