

I B.Tech Supplementary Examinations, Aug/Sep 2007
MATHEMATICAL METHODS

(Common to Electrical & Electronic Engineering, Electronics & Communication Engineering, Computer Science & Engineering, Electronics & Instrumentation Engineering, Bio-Medical Engineering, Information Technology, Electronics & Control Engineering, Computer Science & Systems Engineering, Electronics & Telematics, Electronics & Computer Engineering and Instrumentation & Control Engineering)

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions
 All Questions carry equal marks

1. (a) Find a real root of the equation $f(x)=x+\log x-2$ using Newton Raphson method
 (b) Find $f(22)$ from the following data using Newton's Backward formula

x	20	25	30	35	40	45
y	354	332	291	260	231	204

[8+8]

2. (a) Fit a curve of the form $y = ae^{bx}$ from the following data.

x	1	2	3	4	5	6
y	1.6	4.5	13.8	40.2	125	300

- (b) Evaluate $\int_0^1 e^{-x^2}$ taking $h = .2$ using

i. Simpson's $\frac{1}{3}rd$

ii. Trapezoidal rule.

[8+8]

3. Given $y' = x + \sin y$, $y(0) = 1$ compute $y(0.2)$ and $y(0.4)$ with $h=0.2$ using Euler's modified method

[16]

4. (a) Determine the rank of the matrix.

$$A = \begin{bmatrix} 2 & -1 & 3 & 4 \\ 0 & 3 & 4 & 1 \\ 2 & 3 & 7 & 5 \\ 2 & 5 & 11 & 6 \end{bmatrix} \text{ by reducing it to the normal form.}$$

- (b) Find whether the following equations are consistent, if so solve them.

$$x + 2y - z = 3$$

$$3x - y + 2z = 1$$

$$2x - 2y + 3z = 2$$

$$x - y + z = -1.$$

[8+8]

5. Diagonalize the matrix $\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ [16]
6. (a) Show that every square matrix can be expressed uniquely as a sum of a symmetric and skew symmetric matrices.
- (b) Determine a, b, c so that A is orthogonal where $A = \begin{bmatrix} 0 & 2b & c \\ a & b & -c \\ a & -b & c \end{bmatrix}$ [8+8]
7. (a) Find the half range cosine series for the function $f(x) = (x-1)^2$ in the interval $0 < x < 1$ Hence show that $\sum_{n=1}^{\infty} \frac{1}{(2n-1)^2} = \frac{\pi^2}{8}$
- (b) State and prove Fourier integral theorem. [10+6]
8. (a) Form the partial differential equation by eliminating the arbitrary constants from $(x-a)^2 + (y-b)^2 + z^2 = r^2$
- (b) Solve the partial differential equation $z^2(p^2 + q^2) = x^2 + y^2$
- (c) Find the Z - transform of $\sin \alpha k$, $k \geq 0$ [5+6+5]

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1. (a) Find an iterative formula to find the cube root of a number using Newton's Raphson's method. Hence evaluate cube root of 15
- (b) For $X=20,25,32,49$ and $\cos(x) = 0.939, 0.906, 0.848, 0.656$ find $\cos(43)$ using Lagrange's formula. [8+8]

2. Fit a parabola of the form $y=a+bx+cx^2$

x	1.0	1.5	2.0	2.5	3.0	3.5	4.0
y	1.1	1.3	1.6	2.0	2.7	3.4	4.1

[16]

3. Find $y(.5)$, $y(1)$ and $y(1.5)$, given that $y' = 4-2x$, $y(0) = 2$, with $h = 0.5$ Using Modified Euler method [16]

4. (a) Find the value of K such that the rank of the matrix is 3 $\begin{bmatrix} 1 & 2 & -1 & 3 \\ 4 & 1 & 2 & 1 \\ 3 & -1 & 1 & 2 \\ -1 & 2 & 0 & K \end{bmatrix}$

- (b) Find whether the system of equations $x_1 + 2x_2 + x_3 - 2x_4 = 6$, $2x_1 + 3x_2 + 2x_3 - 2x_4 = 8$, $3x_1 + x_2 + 2x_3 - x_4 = 4$, $4x_1 + 2x_2 + 2x_3 - 3x_4 = 9$ is consistent, if so solve them. [8+8]

5. Diagonalize the matrix $A = \begin{bmatrix} 8 & -8 & -2 \\ 4 & -3 & -2 \\ 3 & -4 & 1 \end{bmatrix}$ [16]

6. (a) Find a real symmetric matrix C of the quadratic form $Q = x_1^2 + 3x_2^2 + 2x_3^2 + 2x_1x_2 + 6x_2x_3$ and find the index and signature.

- (b) Find the orthogonal transformation which transforms the quadratic form $x_1^2 + 3x_2^2 + 3x_3^2 - 2x_2x_3$ to canonical form. [8+10]

7. (a) Obtain a Fourier expansion for $\sqrt{1 - \cos x}$ in the interval $-\pi < x < \pi$.

- (b) If $F(s)$ is the complex Fourier transform of $f(x)$, then prove that
 $F(f(x) \cos ax) = \frac{1}{2} [F(s+a) + F(s-a)]$
 $F[f(x-a)] = e^{isa} F(s)$. [10+6]

8. (a) Form the partial differential equation by eliminating the arbitrary constants $z=f(x^2+y^2+z^2)$.
- (b) Solve the partial differential equation $p^2x + q^2y = z$.
- (c) Solve the difference equation, using Z-transforms $u_{n+2} - u_n = 2^n$ where $u_0 = 0, u_1 = 1$. [5+5+6]

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1. (a) Find a real root of $x^4 - x - 10 = 0$ using bisection method.
 (b) Find $f(9)$ by Newton's Backward formula given that $f(2) = 94.8$, $f(5) = 87.9$, $f(8) = 81.3$, $f(11) = 75.1$. [8+8]

2. (a) By the method of least squares fit a parabola of the form $y = a + bx + cx^2$ for the following data.

x	2	4	6	8	10
y	3.07	12.85	31.47	57.38	91.29

- (b) Derive the formula to evaluate $\int_a^b y dx$ using trapezoidal rule.

- (c) Use the trapezoidal rule with $n=4$ to estimate $\int_0^1 \frac{dx}{1+x^2}$ Correct to four decimal places. [8+4+4]

3. Find the solution of $\frac{dy}{dx} = x - y$ at $x = 0.1, 0.2, 0.3, 0.4$ and 0.5 using modified Euler method. $y(0) = 1$ [16]

4. (a) Determine whether the following equations will have a non-trivial solution if so solve them.

$$3x + 4y - z - 6\omega = 0; \quad 2x + 3y + 2z - 3\omega = 0$$

$$2x + y - 14z - 9\omega = 0; \quad x + 3y + 13z + 3\omega = 0.$$

- (b) Solve the tridiagonal system

$$3x_1 - x_2 = 4,$$

$$2x_1 - x_2 + x_3 = 6,$$

$$2x_2 + 3x_3 + 2x_4 = 11,$$

$$x_3 - 2x_4 = -1$$

by writing the coefficient matrix as a product of a lower triangular and upper triangular matrices. [8+8]

5. Diagonalize the matrix $\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ [16]

6. (a) Prove that every hermitian matrix can be written as $A+iB$ where A is real and Symmetric and B is real and Skew-Symmetric.
- (b) Reduce the quadratic form $x_1^2 + 3x_2^2 + 3x_3^2 - 2x_2x_3$ to a canonical form. [8+8]
7. (a) Write the Dirichlet's conditions for the existence of Fourier series of a function $f(x)$ in the interval $(\alpha, \alpha + 2\pi)$. Find the Fourier series representing $f(x) = x, 0 < x < 2\pi$
- (b) Find the Fourier transform of $f(x) = \begin{cases} 1 - x^2 & \text{if } |x| < 1 \\ 0 & \text{if } |x| > 1 \end{cases}$
- Hence evaluate $\int_0^{\infty} \left[\frac{x \cos x - \sin x}{x^2} \right] \cos \frac{x}{2} dx$. [8+8]
8. (a) Form the partial differential equation by eliminating the arbitrary constants $\log (az - 1) = x + ay + b$.
- (b) Solve the partial differential equation $px(y^2 + z) - qy(x^2 + z) = z(x^2 - y^2)$.
- (c) If $Z(u_n) = \frac{2z^2 + 5z + 14}{(z-1)^4}$, find u_2 and u_3 [5+6+5]

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x	20	25	30	35	40	45
y	354	332	291	260	231	204

[8+8]

2. Fit a parabola of the form $y = A_1e^{\lambda x} + A_2e^{\lambda^2 x}$ for the following data

x	1.0	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8
y	1.175	1.336	1.51	1.698	1.904	2.129	2.376	2.646	2.942

[16]

3. Find $y(1)$, $y(2)$ and $y(3)$ using Taylor's series method that $\frac{dy}{dx} = l - y$, $y(0) = 0$

[16]

4. (a) Find whether the following equations are consistent, if so solve them.
 $x+y+2z = 4$; $2x-y+3z = 9$; $3x-y-z=2$

- (b) Find the rank of the matrix

$$\begin{bmatrix} 1 & 2 & 3 & 0 \\ 2 & 4 & 3 & 2 \\ 3 & 2 & 1 & 3 \\ 6 & 8 & 7 & 5 \end{bmatrix}$$

by reducing it to the normal form.

[8+8]

5. (a) Find the eigen values and the corresponding eigen vectors of the matrix. $\begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$

- (b) If A and B are n rowed square matrices and if A is invertible show that $A^{-1} B$ and BA^{-1} have the same eigen values.

[10+6]

6. (a) Prove that every hermitian matrix can be written as $A+iB$ where A is real and Symmetric and B is real and Skew-Symmetric.

- (b) Reduce the quadratic form $x_1^2 + 3x_2^2 + 3x_3^2 - 2x_2x_3$ to a canonical form. [8+8]

7. (a) Find the Fourier series for $f(x)$; if $f(x)$ is defined in $-\pi < x < \pi$ as
- $$f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ x, & 0 < x < \pi \end{cases}$$
- Deduce that $\frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$
- (b) Find a half range sine series for $f(x)=ax+b$ in $0 < x < 1$
- (c) Find Fourier cosine transform of $f(x) = \begin{cases} \cos x & 0 < x < a \\ 0 & x \geq a \end{cases}$ [6+5+5]
8. (a) Form the partial differential equation by eliminating the arbitrary constants a, b from $2z = (x + a)^{1/2} + (y - a)^{1/2} + b$.
- (b) Solve the partial differential equation., $z^4 p^2 + z^4 q^2 = x^2 y^2$.
- (c) Find $Z^{-1} \left[\frac{z}{z^2+11z+24} \right]$. [5+5+6]
